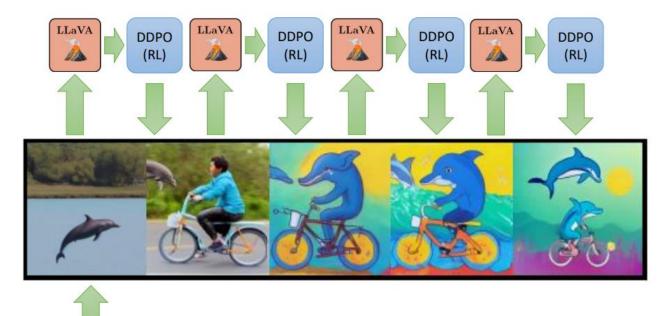
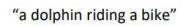
Introduction To Reinforcement Learning





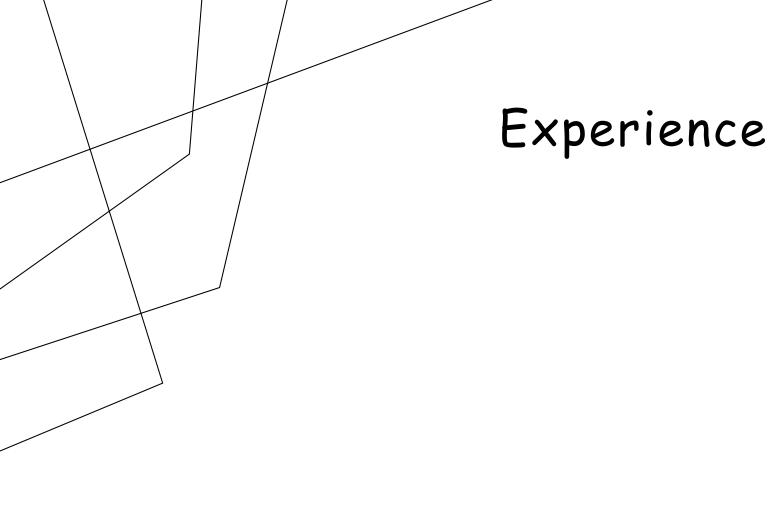
Lancaster Al Reading Group – 22nd January 2025 Based on CS285 Berkeley Course

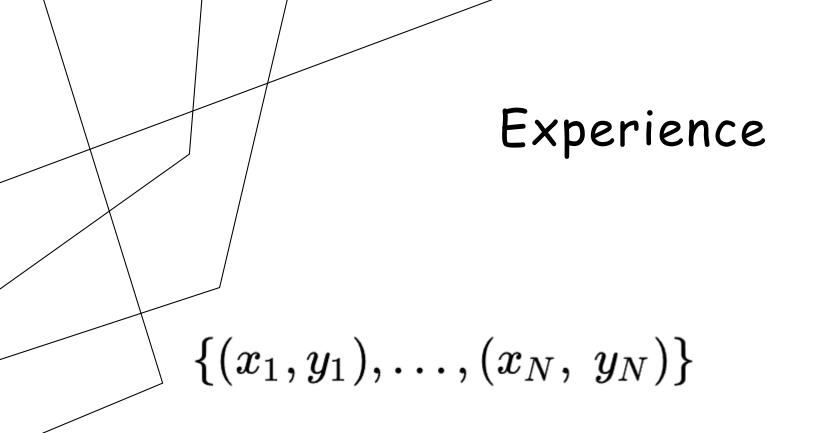


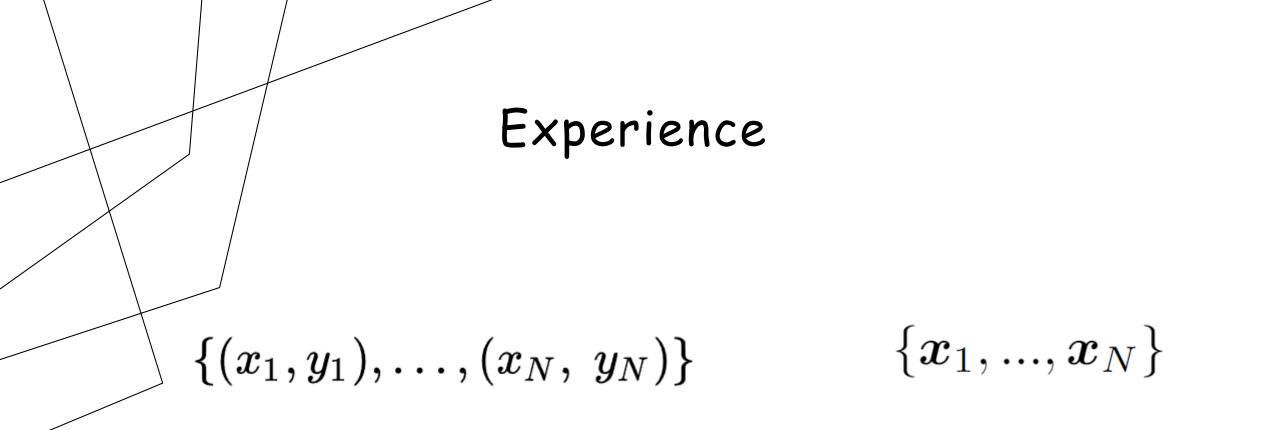
Machine Learning

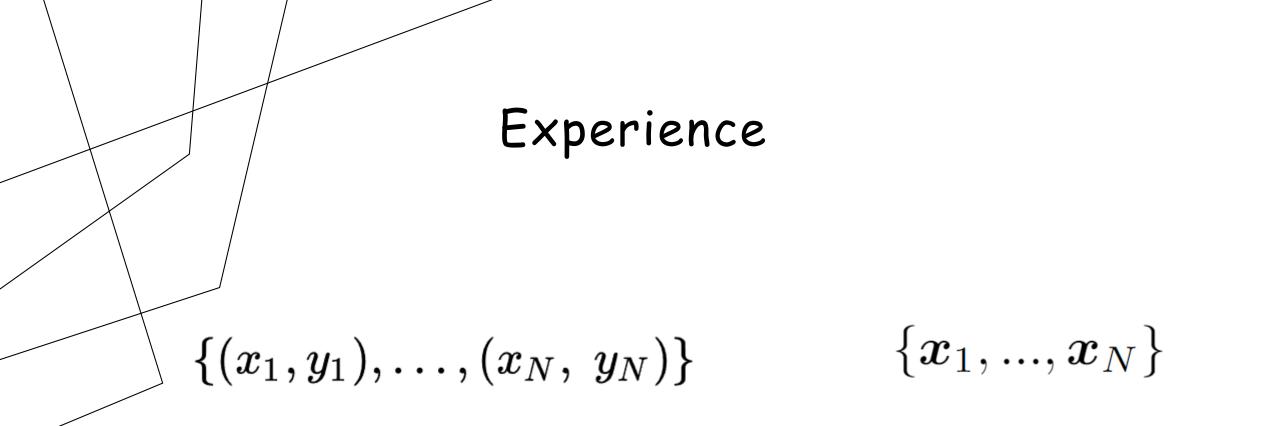
A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P if its performance at tasks in T, as measured by P, improves with experience E.

By Tom Mitchell (Prof. Carnegie Mellon University):









That is not always the case!

Supervised Learning Unsupervised Learning Reinforcement Learning

Supervised Learning Unsupervised Learning Reinforcement Learning

$$\{(x_1, y_1), \dots, (x_N, y_N)\}$$
 $\{x_1, \dots, x_N\}$
Learn p(y|x) Learn p(x)

Supervised Learning Unsupervised Learning Reinforcement Learning

• Environment

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- Environment
- Agent
- Actions
- Rewards

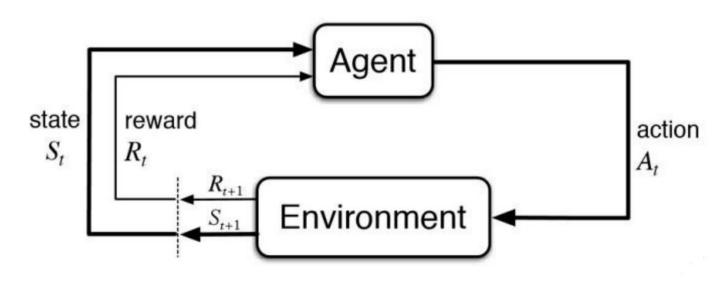
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Learn p(y|x) Learn p(x)

- Environment
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- Rewards

How to learn a policy that maximise the cumulative reward?

The RL Framework

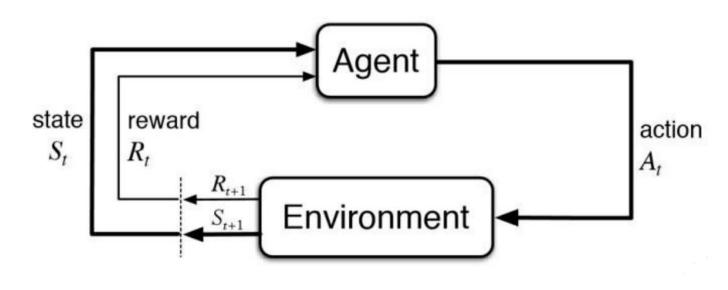


Reinforcement Learning

- Environment
- Agent
- Actions
- Rewards

How to learn a policy that maximise the cumulative reward?

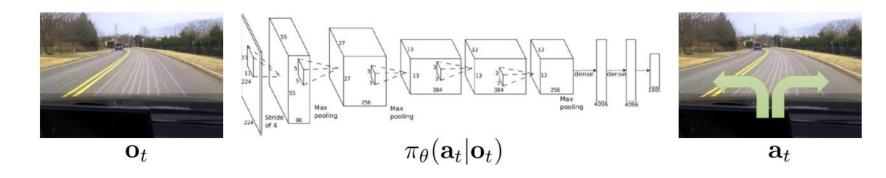
The RL Framework



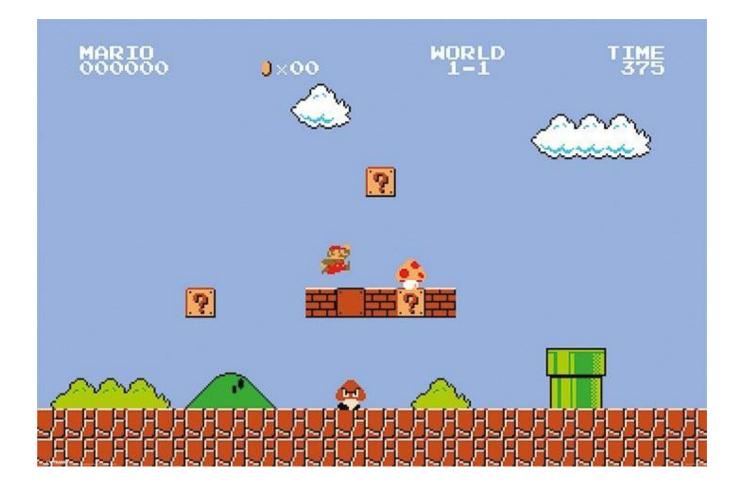
Reinforcement Learning

- Environment
- Agent
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- Rewards

How to learn a policy that maximise the cumulative reward?



RL Examples



RL Examples



Actions: muscle contractions Observations: sight, smell Rewards: food



Actions: what to purchase Observations: inventory levels Rewards: profit



Actions: motor current or torque Observations: camera images Rewards: task success measure (e.g., running speed)

What about the environments?

What about the environments?





What about the environments?

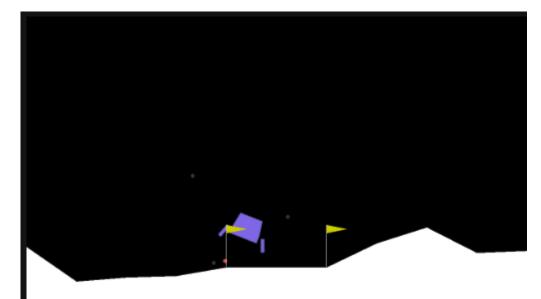


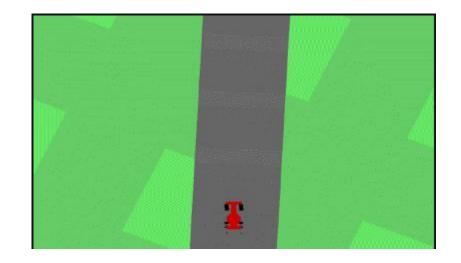
import gym

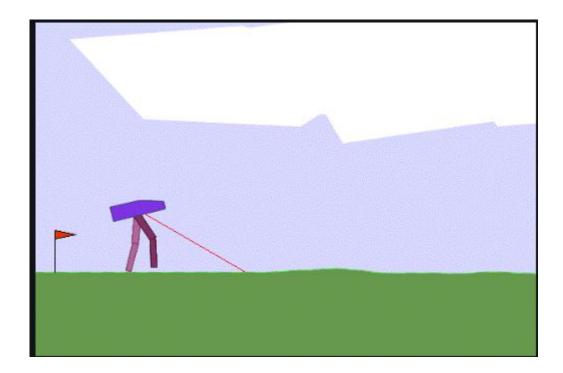
Create an environment env = gym.make("Ant-v4", new_step_api=True) # Reset the environment to an initial state obs = env.reset() # Take a random action action = env.action_space.sample() # Update the environment according to the action obs, reward, done, info = env.step(action)

env.close()

Example Environments









A simple RL algorithm: **REINFORCE**

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• Sample a trajectory from the current policy.

A simple RL algorithm: **REINFORCE** $\nabla_{\theta} \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\sum_{t} r(s_{t}, a_{t}) \right] \approx \frac{1}{N} \sum_{i=1}^{N} \left(\sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(a_{i,t}|s_{i,t}) \right) \left(\sum_{i=1}^{T} r(s_{i,t}, a_{i,t}) \right)$

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- Estimate the gradient of the objective (use backpropagation in the case of Neural Networks).

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- Sample a trajectory from the current policy.
- Estimate the gradient of the objective (use backpropagation in the case of Neural Networks).
- Update the policy using a gradient based optimization algorithm.

The necessity of RL

• Some tasks are hard to get supervised pairs from (e.g. movements of a robot).

The necessity of RL

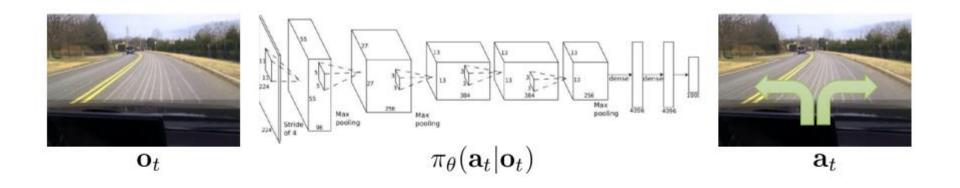
- Some tasks are hard to get supervised pairs from (e.g. movements of a robot).
- Supervised learning is not ideal for sequential decision making.

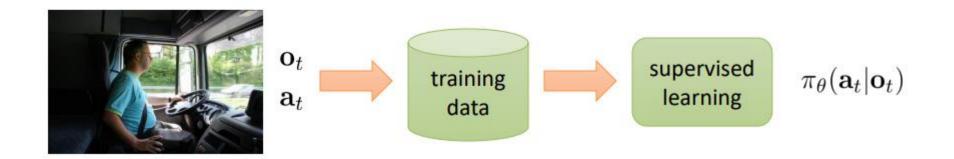
The necessity of RL

- Some tasks are hard to get supervised pairs from (e.g. movements of a robot).
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- RL allows for novel solutions.

Imitation Learning

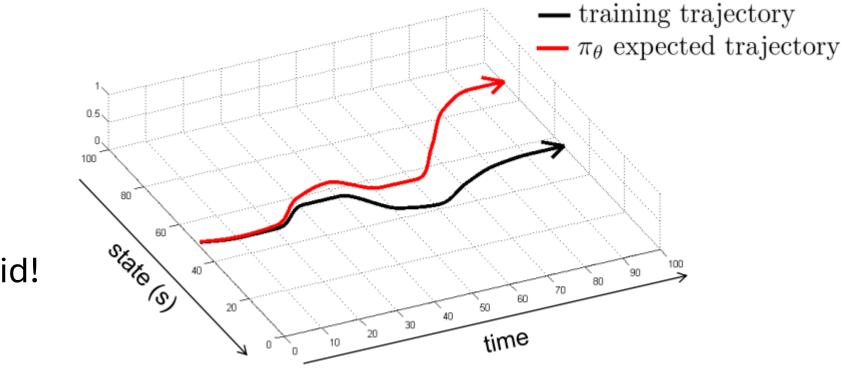
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Imitation Learning

• Supervised learning is not ideal for sequential decision making.



Data is not iid!

• RL allows for novel solutions.



vibrant portrait painting of Salvador Dalí with a robotic half face

a shiba inu wearing a beret and black turtleneck a close up of a handpalm with leaves growing from it





an espresso machine that makes coffee from human souls, artstation panda mad scientist mixing sparkling chemicals, artstation

a corgi's head depicted as an explosion of a nebula



• RL allows for novel solutions.

$$p(x)$$
 $p(x|c)$

$$p(y_n|y_{1:n-1})$$





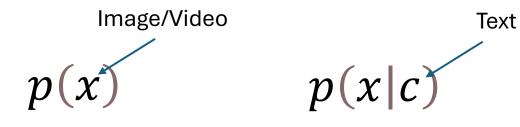


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Next token

Prev tokens

 $p(y_n | y_{1:n-1})$



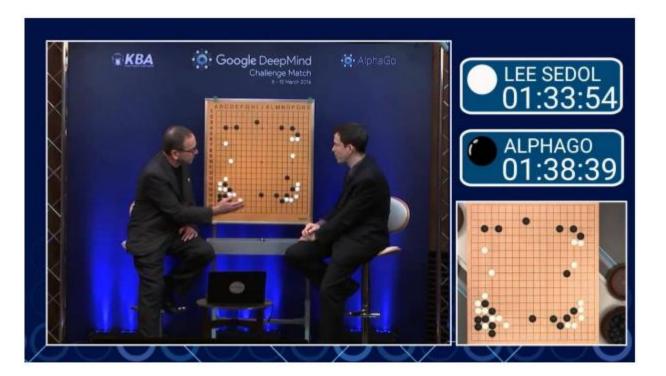
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"Move 37" in Lee Sedol AlphaGo match: reinforcement learning "discovers" a move that surprises everyone

Recent advances in DL vs RL

• RL allows for novel solutions.



"Move 37" in Lee Sedol AlphaGo match: reinforcement learning "discovers" a move that surprises everyone

Impressive because no person had thought of it!

- State at time t: S_t
- Action at time t: a_t
- Reward function: $r(s_t, a_t)$

The Q-Function is the total reward from taking action a_t in state s_t :

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Idea 1: $Q^{\pi}(s_t, a_t) = \sum_{t'=t}^T \mathbb{E}_{\pi_{\theta}}[r(s_{t'}, a_{t'})|s_t, a_t]$ $V^{\pi}(s_t) = \sum_{t'=t}^T \mathbb{E}_{\pi_{\theta}}[r(s_{t'}, a_{t'})|s_t]$ Idea 2: $V^{\pi}(s_t) = \mathbb{E}_{a_t \sim \pi(\alpha_t | s_t)} \left[Q^{\pi}(s_t, a_t)\right]$

Idea 1:

If we have a policy π and we know the Q-Function we can improve the policy by setting:

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$$T$$

$$V^{\pi}(\boldsymbol{s}_{t}) = \sum_{t'=t}^{I} \mathbb{E}_{\pi_{\boldsymbol{\theta}}}[r(\boldsymbol{s}_{t'}, \boldsymbol{a}_{t'}) | \boldsymbol{s}_{t}]$$

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$$\pi'(\boldsymbol{a}|\boldsymbol{s}) = 1 \text{ if } \boldsymbol{a} = \arg \max_{\boldsymbol{a}} Q^{\pi}(\boldsymbol{s}, \boldsymbol{a})$$

$$Q^{\pi}(\boldsymbol{s}_t, \boldsymbol{a}_t) = \sum_{t'=t}^{T} \mathbb{E}_{\pi_{\boldsymbol{\theta}}}[r(\boldsymbol{s}_{t'}, \boldsymbol{a}_{t'}) | \boldsymbol{s}_t, \boldsymbol{a}_t]$$

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Idea 2: If $Q^{\pi}(s, a) > V^{\pi}(s)$ then a is better than average and we can increase $\pi(a|s)$.

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- Policy Gradients:
- Value Based:
- Actor Critic:
- Model-Based:

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- Model-Based: Estimate the transition model and use it for planning/improving policy/other.

$$Q^{\pi}(\boldsymbol{s}_t, \boldsymbol{a}_t) = \sum_{t'=t}^{T} \mathbb{E}_{\pi_{\boldsymbol{\theta}}}[r(\boldsymbol{s}_{t'}, \boldsymbol{a}_{t'}) | \boldsymbol{s}_t, \boldsymbol{a}_t]$$

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Online vs Offline RL

• Online RL: The agent interacts with the environment during training.

Online vs Offline RL

- Online RL: The agent interacts with the environment during training.
- Offline RL: The agent uses a fixed dataset of previously collected experiences without further interaction with the environment during the training phase.

On-Policy vs Off-Policy RL

• On-Policy RL: The agent improves the policy currently being used to make decisions.

On-Policy vs Off-Policy RL

- On-Policy RL: The agent improves the policy currently being used to make decisions.
- Off-Policy RL: The agent improves a different policy than the one it is using.

Exploration vs. Exploitation

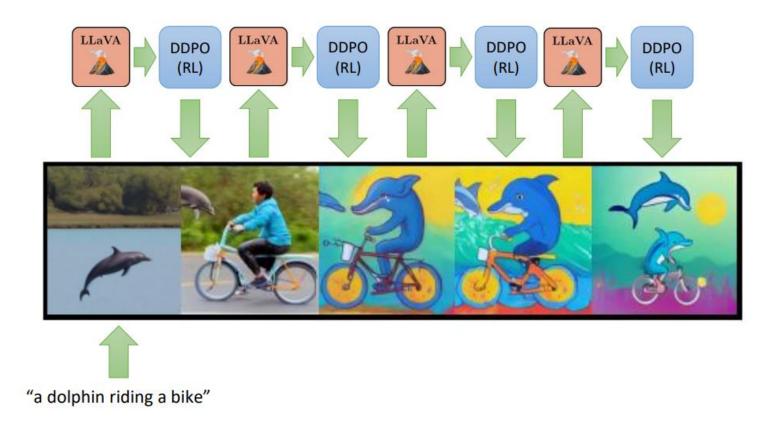
- Exploitation: Go to your favorite restaurant.
- Exploration: Try a new restaurant.

Exploration vs. Exploitation

- Exploitation: Go to your favorite restaurant.
- Exploration: Try a new restaurant.
- Exploitation: Doing what you know will yield highest reward.
- Exploration: Doing things you haven't done before, in the hopes of getting even higher reward.

Exploration vs. Exploitation

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Kevin Black, Michael Janner, Yilun Du, Ilya Kostrikov, Sergey Levine. Training Diffusion Models with Reinforcement Learning. 2023.

Imitation-based policies can be sensitive



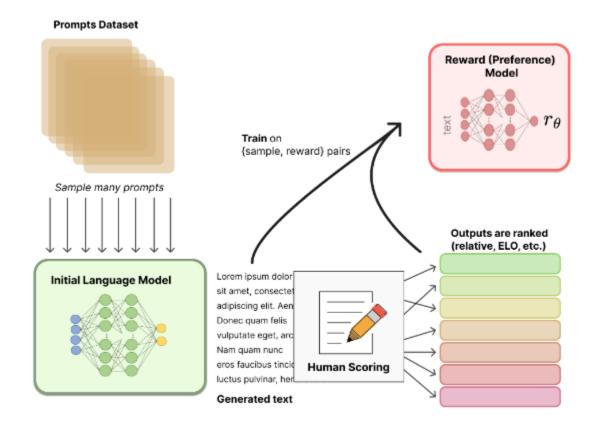
source policy (motion imitation)

Smith et al., "Learning and Adapting Agility Skills by Transferring Experience." 2022.

RL for fine-tuning LLMs

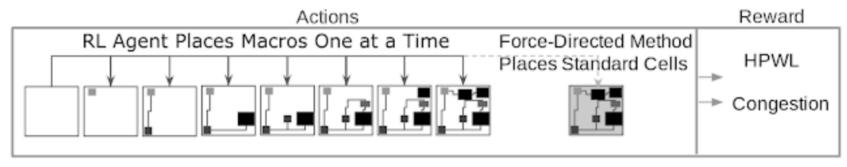
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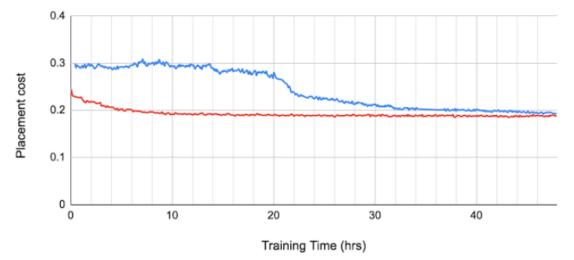


Source: https://huggingface.co/blog/rlhf

RL for Chip Design

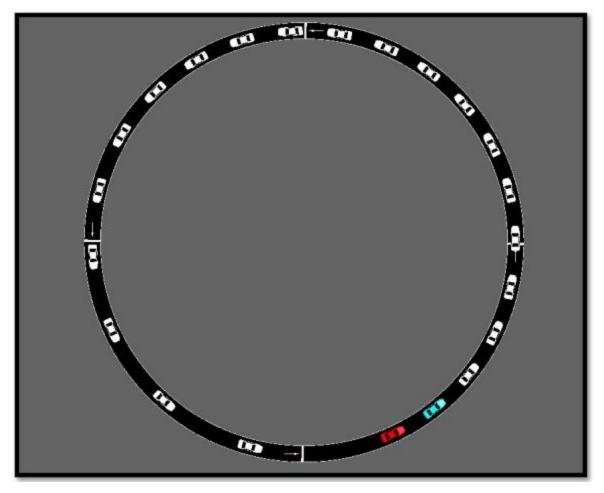


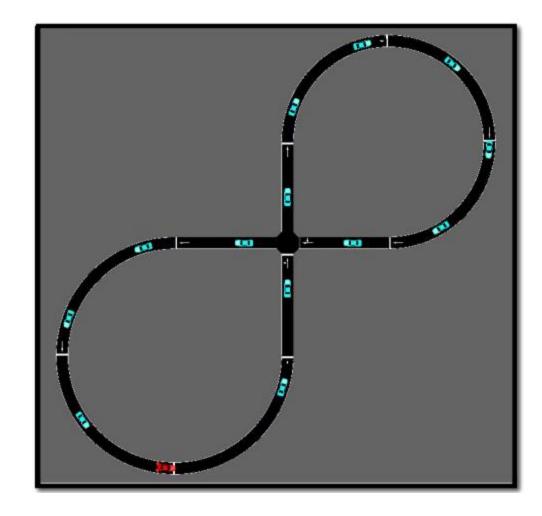
- From Scratch - Finetune a Pre-trained Policy



Source: https://ai.googleblog.com/2020/04/chip-design-with-deep-reinforcement.html

RL for Controlling Traffic





Wu Cathy et al., Emergent Behaviors in Mixed-Autonomy Traffic, 2017